## Cross-Layer Design for Wireless Communications

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# Schedule

- Lecture class : 10h
- Lecture slot (exercises included) : 2h
- Evaluation :
  - 1 Test duration 2h scheduled on the 02/02/2015 at 10h00

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# Outline

- Part I : Layered architectures
- Part II : PHY/MAC resource allocation and system models
- Part III : A cautionary perspective of cross-layer design

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# Bibliography

- These lecture notes have been produced with the following materials
  - Ana I. Pérez-Neira, Marc Realp Campalans, "Cross-Layer Resource Allocation in Wireless Communications", *Elsevier*,
  - Marvin K. Simon, Mohamed Slim-Alouini, "Digital Communication Over Fading Channels", Wiley,
  - Jean-Marie Gorce, "Les technologies 802.11 pour les réseaux sans-fil" *INSA de Lyon*.
  - David Tse, Pramod Viswanath "Fundamentals of Wireless Communications"
  - several research articles

## Aim of the course

- New doors on wireless system designs
- Focus to radio systems
- Cross-layer => Interaction between several layers (OSI)
  - PHY Layer (physical layer)
  - MAC Layer (medium access control layer)
  - Network Layer
- What we need to know
  - Difference between a cross-layer architecture and a layered architecture
  - Wireless systems characteristics => multi-users, interference
    - PHY : noise, fading, interference,
    - MAC : channel access, congestion management (interference)
    - Network : routing, high level interference (Network architecture dependent)

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#### Introduction

- Definition : A communication network is a set of electronic devices (nodes) connected to each other following some rules (routing)
- Two important characteristics for a network
  - Transmission technology
    - Broadcasting : TV num, Radio
    - Point to point network (communication networks : Cellular, sensor networks, ...)
  - Scale
    - BAN (Body Area Networks)
    - PAN (Personal Area Networks) Office
    - LAN (Local Area Networks) building, campus
    - MAN (Metropolitan Area Networks) Town
    - WAN (Wide Area Networks) Country, continent
    - Internet Planet

#### Communication network

- Every packet has an unique or a finite number of destinations
- Direct link (1 hop) : A radio link exists (?) between two nodes;
- Multi-hop communications : the source cannot reach the destination in one hop
  - A specific route is needed (Which criteria?)
  - Depends on the cost function (distance, energy, latency, loss probability, ...)
- Routing algorithm
  - pro-active
  - reactive

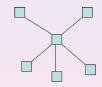
**Definition and Generality** 

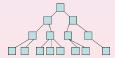
## Topology

- Bus : Wired network of computer
- Star : Cellular, WLAN, etc.

• Tree : hierarchical architecture







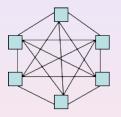
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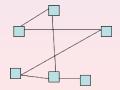
**Definition and Generality** 

# Topology (cc'ed)

- Ad-hoc network : connected nodes without an infrastructure
  - Fully connected



Partially connected



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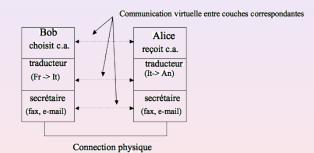
**Definition and Generality** 

### Layered Protocol Architecture

- The networks are built according layers above to each other
- "Divide and Conquer" approach
  - Separate the functionalities => reduced complexity
- Aim of each layer : provides services to the upper layers whilst hiding implementation issues for the upper layers.
- Definition : the set of layers and protocols is called network architecture

## The birthday card

 Bob (French) wishes sending a birthday card to Alice (American), and uses an agency for the translation



• The layer *n* communicates with the associated layer by a set of rules called layer *n* protocol

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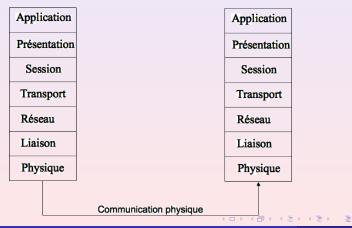
## Functionalities of the birthday card

- layer 1 protocol : fax
  - Dealt with the same layer at the destination
  - Can be changed to e-mail
- layer 2 protocol : intermediate translate language
  - italian can be switched in chinese or spanish
- Each layer adds informations which can be read only by the same layer at the destination
  - addition of header and/or tailer to packets
- Important properties for a layered architecture :
  - Each layer performs a set of functions
  - The information flow between layers must be minimized
  - How many layers should we design?
    - few => too many functionalities per layer
    - a lot => complex architecture

**Definition and Generality** 

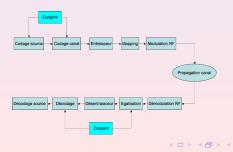
# OSI model

- OSI : Open Systems Interconnection
  - Alternate models e.g. TCP/IP
- 7 different layers



## OSI layers : PHY layer

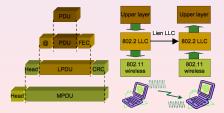
- Function : information transmission (bits) in a noisy channel
- Main design functions :
  - representation of "0" and "1"
  - bit duration
  - transmission type (simplex, duplex)
  - how to start/finish a connection
  - source/channel coding, etc.



## OSI layers : Data link layer

Can be separated in two sub-layer, i.e. Logical Link Layer (LLC) and Medium Access Control (MAC)

- First error-free layer
- LLC
  - Interface between the MAC and the network layer (3)
  - Data exchange between users in a LAN
  - Data link layer error control : retransmission of packets (ARQ)
  - $\bullet\,$  The above layer is waiting for an error-free transmission service (i.e. TCP/IP)



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## OSI layers : Data link layer

The MAC layer manages the medium access between users

- Interface between the LLC and the PHY layer
- Frame addressing (physical address)
- Allow to be associated to a network
- Medium access manager
  - Avoid and detect collisions (CSMA/CD, ex : Ethernet)
  - Wireless channel : no collision detection => CSMA/CA (WLAN)
  - ALOHA protocol
  - Resource allocation in centralized networks (TDMA, FDMA, CDMA, etc.)

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## OSI layers : Network layer

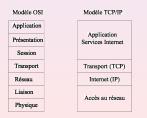
- Routing packets from a source to a destination
- Universal addressing, e.g. IPv4
- Congestion control (too many request on a particular node)
- Connected mode : a link should be established before sending a packet between two nodes. Packet order saved
- Non connected mode : "postal card" mode => every packet carries the destination address; independent routing
- Commutation (connected) : one route is computed once for all
- Routing (non connected) : a route is established for each packet

## OSI Layers : Transport Layer

- The last layer before the applications layers
- Reliable end-to-end information delivery
- Main function : rearrange in small packets the data from the session layer and ensure that they are delivered at the destination
  - Control Mechanism of error and flow
- Provides services for connected and non-connected mode
- Connected mode => Packets can be rearranged (TCP/IP)
- TCP can be included in the Transport Layer

## **OSI model : Applications Layers**

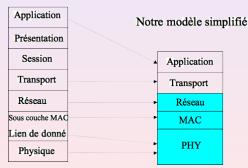
- Session Layer (5) : Advanced services, dialogues management. Turns on, manages and finishes the remote connections
- Presentation Layer (6) : Convert in bytes the syntax and semantic of the application layer for the other layers of the OSI stack
- Application Layer (7) : The closest to the user. Interacts with the application software



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#### Simplified OSI model

• Only the first three layers will be considered



Modèle OSI

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**Definition and Generality** 

## Advantages of layered architectures

#### Modularity

- Simplicity
- Easy debugging
- Standardization
- Development time reduced for the new protocols
- Is there any inconvenient with the layered architecture?
  - Assumption : the layers can be optimized independently from each other
    - Limit in the wireless case?
    - Is it efficient?
    - What is the other solutions?
  - Do not forget : a wireless network does not include the links !

#### Cross-layer design

#### Advantages

- Exploit the interaction between the layers
- In wireless : Dependency between layers and their functionalities
- Disadvantages
  - The interactions between protocols from several layers are difficult to model
  - Probably lead to complex algorithms
  - Is the modularity conserved ?
- X-layer design : understanding and exploitation of the interactions between layers

#### Cross-Layer vs Layered

- Should the OSI model be rejected if we talk about x-layer?
- Do we need of a network architecture?
- Is the x-layer design suitable for any type of networks and all kind of application ?

The layered architecture cannot be rejected and all layers cannot be optimized together without any frontiers

- "spaghetti code"
- No way to make it sustainable

Solution => Holistic view of wireless networks

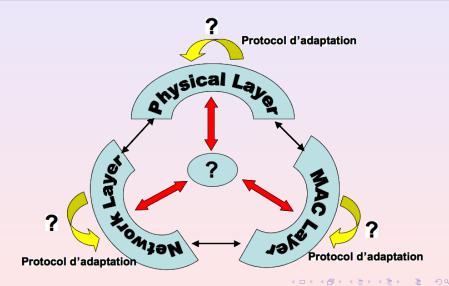
#### Cross-layer design

Let us focus on the first three layers

- Derive an abstract model for each layer and QoS criteria
- Design adaptive protocols at each level
- What are the needed exchanges between each pair of layers
- Obtain a tradeoff between performances, complexity and scaling

Definition and Generality

#### Cross-layer design



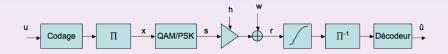
## Design criteria

- Several QoS criteria according to the layer
- PHY
  - BER, capacity/throughput, PER, SINR
- MAC
  - Channel access delay, throughput without error
- Network
  - Delay, throughput, rejection probability
- Other criteria
  - Energy consumption (Devices / network life duration)
  - Utility of a user
  - => Every layer concerned

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PHY models Spectral Efficiency

## Capacity

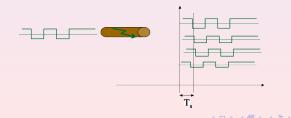


- The output signal is :  $r = h \cdot s + w$  et  $w \sim \mathcal{CN}(0, \sigma^2)$
- The capacity of the channel is  $C(\gamma) = \log_2(1+\gamma)$  bits/s/Hz

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## Wireless link characteristics

- QoS PHY criteria : BER
- BER depends on the received power (fading, selective channels, ...), coding, components, etc.
- Channel : Fading + shadowing + pathloss.  $P_r = P_t \cdot PL \cdot \alpha_{shad} \cdot |h|^2$
- Multi-user  $\implies$  interference
- Flat Fading :  $\tau_{\max} < T_s$ 
  - Random summation of many paths



PHY models Spectral Efficiency

## Bit Error Rate (BER) in AWGN

- Important criterium for a non-coded modulation scheme (M-QAM, M-PSK)
- Exact expression for M-QAM and M-PSK quite hard to obtain => approximations

$$BER_{MQAM}(\gamma) \approx 4\left(1-\frac{1}{\sqrt{M}}\right)\frac{1}{\log_2 M}\sum_{i=0}^{\sqrt{M/2-1}}Q\left((2i+1)\sqrt{\frac{3\gamma}{M-1}}\right)$$
$$BER_{MPSK}(\gamma) \approx \frac{2}{\max(\log_2 M, 2)}\sum_{i=1}^{\max(M/4, 1)}Q\left(\sin\frac{(2i-1)\pi}{M}\sqrt{2\gamma}\right)$$

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#### Instantaneous and average SNR

- Base band and flat fading channel : y(t) = h(t)x(t) + n(t)
  - h(t) is a single complex coefficient (gaussian for instance) and constant over one symbol : h(t) = α(t)e<sup>jθ(t)</sup>
- instantaneous SNR (over one symbol) :

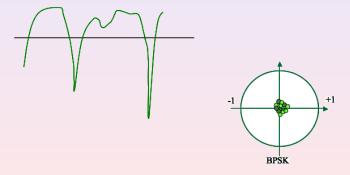
$$\gamma(t) = \frac{E\left[|h(t)x(t)|^2\right]}{E\left[|n(t)|^2\right]} = \alpha(t)^2 \frac{E_s}{N_0}$$

• Average SNR :

$$\overline{\gamma}(t) = E[\gamma(t)] = E[\alpha(t)^2] \frac{E_s}{N_0} = \Omega \frac{E_s}{N_0}$$

# Rayleigh channel

• NLOS channel : summation of random variables with random phase and module



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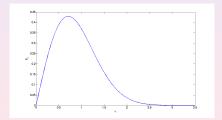
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PHY models Spectral Efficiency

# Rayleigh Fading

• The channel magnitude modelized by a Rayleigh law

$$p_{\alpha}(\alpha) = \begin{cases} \frac{2\alpha}{\Omega} \exp\left(-\frac{\alpha^{2}}{\Omega}\right) & \alpha \ge 0\\ 0 & \text{elsewhere} \end{cases}$$



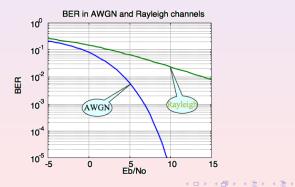
• The law of the SNR is  $p_{\gamma}\left(\gamma
ight)=rac{1}{\overline{\gamma}}e^{-rac{\gamma}{\overline{\gamma}}}$ 

PHY models Spectral Efficiency

## Fading effect on the BER

• The instantaneous SNR is time varying => error probability also :

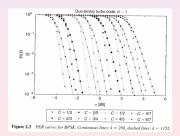
$$P_{b}(E) = \int_{0}^{\infty} P_{b}(E|\gamma) p_{\gamma}(\gamma) d\gamma = \frac{1}{2} \left[ 1 - \sqrt{\frac{\overline{\gamma}}{1 + \overline{\gamma}}} \right]$$



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# Packet Error Rate (PER)

- Real systems : mapping + modulation and coding scheme (MCS)
- Effective transmission rate (information) :  $R^{(m)} = b^{(m)}c^{(m)}$
- Decoded bits are passed to the MAC/Link
  - Received packet at PHY with a non zero PER. Depends on m (MCS) and  $\gamma => PER^{(m)}(\gamma)$
  - Transmission probability :  $PSR^{(m)}(\gamma) = 1 PER^{(m)}(\gamma)$



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PHY models Spectral Efficiency

# MAC/Link Throughput

- Shannon capacity : Optimal MCS without errors
- Transmission errors  $= PER \neq 0$
- Amount of data without errors delivered from MAC/Link to the above layers at t :

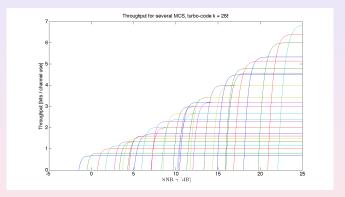
$$\eta^{(m)}(\gamma) = \mathsf{R}^{(m)}\mathbf{1}\left\{Z_{i}=1\right\}$$
 bits / channel use

Instantaneous value varying in time (even though γ constant!)
 Throughput : η
<sup>(m)</sup>(γ) = E<sub>t</sub> [η<sup>(m)</sup>(γ)] = R<sup>(m)</sup>PSR<sup>(m)</sup>(γ)

OSI Model PHY/MAC characteristic Resource allocation

PHY models Spectral Efficiency

## Throughput vs MCS



• Not all the MCS are interesting !

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## Link adaptation

- System abilities to match MCS, power to the radio link quality
  - Radio link quality : SNR (SINR with interference)
- MCS adaptation to optimize a cost function (e.g. BER, throughput, etc.)
- Cross-layer => throughput maximization MAC/Link (e.g. HSDPA)
- CSI (Channel State Information) is needed at the transmitter
  - TDD system => Symmetry on the channel

## Link Adaptation (cc'ed)

• Ideal feedback channel + SNR known at Tx

$$\overline{\eta}^{(m)}(\gamma) = R^{(m^*)} PSR^{(m^*)}(\gamma) \tag{1}$$

• The optimal MCS is given by :

$$m^* = rg\max_m R^{(m)} PSR^{(m)}(\gamma)$$

• Assumption :  $R^{(m-1)} < R^{(m)} < R^{(m+1)}$ ,  $\exists \gamma^{(m)}_{th}$  such as :

$$R^{(m-1)}PSR^{(m-1)}\left(\gamma_{th}^{(m)}\right) = R^{(m)}PSR^{(m)}\left(\gamma_{th}^{(m)}\right)$$
(2)

• Optimal MCS belongs to :  $\gamma \in \left[\gamma_{th}^{(m)}, \gamma_{th}^{(m+1)}
ight)$ 

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# Link Adaptation (cc'ed)

• The SNR threshold is the level where the throughput curves cross, eq. (2)

m	1	2	3	4	5	6	7	8
	$\left(1,\frac{1}{3}\right)$	$\left(2,\frac{1}{2}\right)$	$\left(2,\frac{3}{4}\right)$	$\left(4,\frac{1}{2}\right)$	$\left(4,\frac{3}{4}\right)$	$\left(6,\frac{2}{3}\right)$	$\left(6, \frac{6}{7}\right)$	$\left(8,\frac{4}{5}\right)$
Rate $R^{(m)}$ $k = 288, \gamma_{\text{th}}^{(m)}$	0.33	1 0.7 dB	1.5 4.2 dB	2 6.6 dB	3 10.3 dB	4 14.1 dB	5.14 17.9 dB	6.4 22 dB
$k = 1152, \gamma_{\mathrm{th}}^{(m)}$		0.9 dB	4.1 dB	6.5 dB	10.2 dB	13.9 dB	17.7 dB	21.8dB

 Table 2.2
 SNR thresholds for throughput maximization.

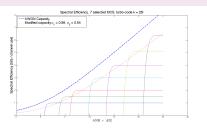
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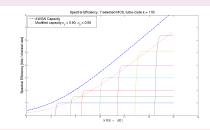
## Analytical approximation of the throughput envelope

- Equation (1) is the throughput envelope
- It can be approached empirically :

$$\overline{\eta}\left(\gamma\right) = \alpha_1 \log_2\left(1 + \alpha_2 \gamma\right)$$

•  $\alpha_1$ ,  $\alpha_2$  depends on the MCS number





# Link Adaptation with QoS constraint

- VoIP, streaming => transmission with QoS certified
- PHY, MAC/Link => PSR minimum, minimum throughput, délai max
- Taking into account the QoS, eq. (1) becomes :

$$\overline{\eta}^{(m)}(\gamma) = R^{(m^*)} PSR^{(m^*)}(\gamma)$$

• with : 
$$m^* = \arg \max_{m} R^{(m)} PSR^{(m)}(\gamma)$$
  
• s.t.  $PSR^{(m)}(\gamma) \ge PSR_{QoS} \iff \gamma \ge \gamma_{QoS}^{(m)}$ 

# Ergodic Spectral Efficiency

- Time varying radio channel
- If the fading is ergodic => ergodic capacity

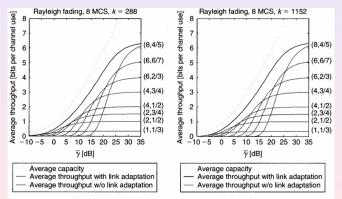
$$\overline{C} = E_{\gamma} \left[ \log_2 \left( 1 + \gamma \right) \right]$$

- Sufficiently long code words in order to encompass all fading states (true if fast fading)
- Slow fading channel => outage probability
- Similar definition for the average throughput

$$\overline{\eta} = E_{\gamma} \left[ R^{(m^*)} PSR^{(m^*)} \left( \gamma \right) \right]$$

## Average Throughput in Rayleigh fading

• Fading => smooth throughput compared to the gaussian case



**Figure 2.9** Average throughput in Rayleigh fading channel with link adaptation (8 MCS) and without link adaptation.

#### problem statement

- Spectral efficiency region : set of achievable data rate
- Tradeoff between the individual spectral efficiency of each user in competition for the channel access
- Resource allocation : scheduling strategies, prioritizing policy, physical resource management between users
- What physical resources can be shared between users?
  - Nature gives us four degrees of freedom : time, frequency, power and space... is that all? (to be cc'ed)

## Signal model for multi-user SIMO multiple access channel

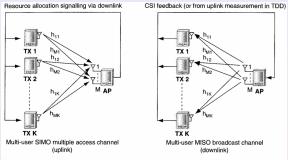


Figure 3.1 Multi-user SIMO multiple access (left) and MISO broadcast (right) channels.

• Aim : optimize the achievable rate region under constraints

$$r = Hs + w$$

## Signal model (cc'ed)

• AP : processing by 
$$V \in \mathbb{C}^{M imes K}$$
 et  $y = V^t Hs + z$ 

• the *k*-th entry of the received signal is :

$$y_k = v_k^t h_k s_k + \sum_{k' \neq k} v_k^t h_{k'} s_{k'} + z_k$$

• The SINR of the user k is :

$$\gamma_{k} = \frac{\left| \boldsymbol{v}_{k}^{t} \boldsymbol{h}_{k} \right|^{2} \boldsymbol{p}_{k}}{\sum_{\substack{k' \in \mathbb{K} \\ k' \neq k}} \left| \boldsymbol{v}_{k}^{t} \boldsymbol{h}_{k'} \right|^{2} \boldsymbol{p}_{k'} + \sigma^{2}}$$

• 
$$\mathbb{K} = \{k \mid k \in \{1, \cdots, K\}; p_k > 0\}$$

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## Successive Interference Cancelation (SIC)

- If all users are decoded in the same time
  - near-far effect problem
  - Interferer like noise => suboptimal
- SIC receiver : decode each entry of **s** by removing all decoded entries from the received signal
  - Iterative receiver
  - Decode users by decreasing power order
- SIC decoding order :  $\pi = {\pi_1, \dots, \pi_K}$ .  $\pi_i = k \Longrightarrow$  the user k is the i-th to be decoded

#### SIC receiver at the AP

$$y_{k}^{SIC} = v_{k}^{t}h_{k}s_{k} + \sum_{\substack{k' \in \mathbb{K} \\ k' \neq k}} v_{k}^{t}h_{k'}s_{k'} - \sum_{\substack{k' \in \mathbb{K} \\ k' \in \{\pi_{1}, \dots, \pi_{i-1}\}}} v_{k}^{t}h_{k'}\hat{s}_{k'}^{SIC} + z_{k},$$
  
$$= v_{k}^{t}h_{k}s_{k} + \sum_{\substack{k' \in \mathbb{K} \\ k' \in \{\pi_{i+1}, \dots, \pi_{K}\}}} v_{k}^{t}h_{k'}s_{k'} + z_{k}$$

- $\hat{s}_{k'}^{SIC}$  current symbol guess with  $y_{k'}^{SIC}$
- Inconvenient
  - may be error propagation

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# Downlink

- Multi-user broadcast channel MISO
- Precoding strategies => User's CSI feedback to the AP
- Broadcast : signal  $s_k$  and interferer  $s_{k'}$  experience the same channel
- The user k receives :

$$y_k = h_k^{(I)} v_k s_k + \sum_{\substack{k' \in \mathbb{K} \\ k' \neq k}} h_k^{(I)} v_{k'} s_{k'} + z_k$$

• Precoding matrix **V** very important (e.g. Dirty Paper Coding)

## Power resource allocation policy

- The SINR of each user depends on  $p_k$  and H
- Block fading (constant channel during T seconds)
- Resource allocation policy : each channel realization => power allocation p (H) = {p<sub>1</sub>, · · · , p<sub>k</sub>}
- The transmitting power is limited
  - Downlink :  $\sum_{k=1}^{K} p_k \leq P_t$
  - Uplink :  $p_k \leq P \ \forall k \in \{1, \cdots, K\}$
- The power resource allocation is  $P = \{p(H) : H \in \mathbb{C}^{M \times K}\}$

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## Resource Allocation and Spectral Efficiency

- Let put  $R_k(\mathbf{H}, \mathbf{p}(\mathbf{H}))$  : shannon capacity or user k throughput
- Average Spectral Efficiency Region : Set of the individual average spectral efficiency which can be obtained via a resource allocation policy
- Power resource allocation policy **P**, the average spectral efficiency vector is :

$$\overline{\mathbf{R}} = \{ E \left[ R_1 \left( \mathbf{H}, \mathbf{p} \left( \mathbf{H} \right) \right) \right], \cdots, E \left[ R_{\mathcal{K}} \left( \mathbf{H}, \mathbf{p} \left( \mathbf{H} \right) \right) \right] \}$$

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#### Achievable data rate region

• Set of the achievable spectral efficiency

$$S = \bigcup_{\mathbf{P} \in \mathbb{P}} \bigcup_{\pi \in \Pi} \left\{ \overline{\mathbf{R}} : \overline{R}_{k} = E\left[ R_{k}\left(\mathbf{H}, \mathbf{p}\left(\mathbf{H}\right) \right) \right], k \in \{1, \cdots, K\} \right\}$$

Π is the set of permutations of {1, · · · , K} (decoding order)
The convex hull S defined the spectral efficiency region :

$$\Omega = \left\{ \sum_{k=1}^{K} \theta_k \overline{R}_k \mid 0 \le \theta_k \le 1, \sum_{k=1}^{K} \theta_k = 1, \overline{R}_k \in S, k \in \{1, \cdots, K\} \right\}$$

## Optimization and region boundaries

• The boundary of  $\Omega$  can be achieved by a vector  $\boldsymbol{\theta} = \{\theta_1, \cdots, \theta_K\}$ 

$$p_{\theta}^{*}\left(\mathbf{H}\right) = \arg \max_{\mathbf{p}(\mathbf{H})} \left( \max_{\pi} \sum_{k=1}^{K} \theta_{k} R_{k}\left(\mathbf{p}\left(\mathbf{H}\right), \mathbf{H}\right) \right)$$

- Let  $\overline{\mathbf{R}_{\theta}^{*}} = \left\{ \overline{R}_{1}^{*}, \cdots, \overline{R}_{K}^{*} \right\}$  the optimal spectral efficiencies for  $\boldsymbol{\theta}$
- No general relationship between  $\theta$  et  $\overline{\mathsf{R}^*_{ heta}}$  can be derived
- The hyperplane  $\sum_{k=1}^{K} \theta_k \overline{R}_k = cst$  is tangent to the boundary of  $\Omega$  at  $\left\{\overline{R}_1^*, \cdots, \overline{R}_K^*\right\}$

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#### Spectral efficiency region for two users

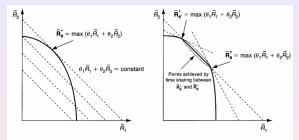


Figure 3.2 Two-user average spectral efficiency region and maximum weighted sum rate.

- For a certain constant value, the bound is achieved
- A same straight line can be tangent to several points

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# Some interesting functioning points

